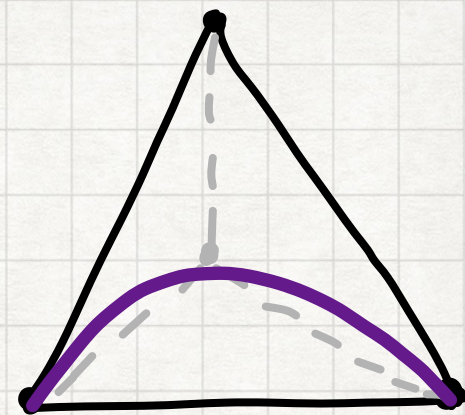


Example 3.2.9: Binomial Random variable



- Consider a biased coin, $P(H) = \theta$, $P(T) = 1 - \theta$

X = "number of heads in two trials"

$$\mathcal{B}_2 = \{ ((1-\theta)^2, 2(1-\theta)\theta, \theta^2) : 0 \leq \theta \leq 1 \} \rightarrow \text{Parametric Description}$$

$$= \{ (p_0, p_1, p_2) \in \mathbb{R}^3 : p_0 + p_1 + p_2 = 1, p_2^2 - 4p_1p_3 = 0, p_0, p_1, p_2 \geq 0 \} \rightarrow \text{Implicit Description.}$$

- Suppose we have two coins C_1, C_2 , we select one at random, toss the coin twice and record # of heads, Y

$$\begin{aligned} P(Y=0) &= \underbrace{P(C=C_1)}_{\lambda} \underbrace{P(X_{C_1}=0)}_{(1-\theta_1)^2} + \underbrace{P(C=C_2)}_{(1-\lambda)} \underbrace{P(X_{C_2}=0)}_{(1-\theta_2)^2} \\ &= \lambda \cdot (1-\theta_1)^2 + (1-\lambda)(1-\theta_2)^2 \end{aligned}$$